# NCERT Solutions Class 12 Maths Chapter 1 Exercise 1.1

## **Question 1:**

Determine whether each of the following relations are reflexive, symmetric and transitive.

(i) Relation R in the set  $A = \{1, 2, 3, \dots, 13, 14\}$  defined as

$$R = \{(x, y) : 3x - y = 0\}$$

- (ii) Relation R in the set of N natural numbers defined as  $R = \{(x, y) : y = x + 5 \text{ and } x < 4\}$
- (iii) Relation R in the set  $A = \{1, 2, 3, 4, 5, 6\}$  defined as  $R = \{(x, y) : y \text{ is divisible by } x\}$
- (iv) Relation R in the set of Z integers defined as
  - $R = \{(x, y) : x y \text{ is an integer}\}$
- (v) Relation R in the set of human beings in a town at a particular time given by
  - (a)  $R = \{(x, y) : x \text{ and } y \text{ work at the same place}\}$
  - (b)  $R = \{(x, y) : x \text{ and } y \text{ live in the same locality} \}$
  - (c)  $R = \{(x, y) : x \text{ is exactly 7cm taller than } y\}$
  - (d)  $R = \{(x, y) : x \text{ is wife of } y\}$
  - (e)  $R = \{(x, y) : x \text{ is father of } y\}$

# Solution:

(i)  $R = \{(1,3), (2,6), (3,9), (4,12)\}$ 

R is not reflexive because (1,1), (2,2)... and  $(14,14) \notin R$ . R is not symmetric because  $(1,3) \in R$ , but  $(3,1) \notin R$ .[since  $3(3) \neq 0$ ]. R is not transitive because  $(1,3), (3,9) \in R$ , but  $(1,9) \notin R$ .[ $3(1)-9 \neq 0$ ]. Hence, R is neither reflexive nor symmetric nor transitive.

(ii)  $R = \{(1,6), (2,7), (3,8)\}$ 

R is not reflexive because  $(1,1) \notin R$ .

R is not symmetric because  $(1,6) \in R$  but  $(6,1) \notin R$ . R is not transitive because there isn't any ordered pair in R such that  $(x,y), (y,z) \in R$ , so  $(x,z) \notin R$ .

Hence, R is neither reflexive nor symmetric nor transitive.

(iii)  $R = \{(x, y) : y \text{ is divisible by } x\}$ We know that any number other than 0 is divisible by itself. Thus,  $(x, x) \in R$ So, R is reflexive. (2,4) ∈ R [because 4 is divisible by 2]
But (4,2) ∉ R [since 2 is not divisible by 4]
So, R is not symmetric.
Let (x, y) and (y,z) ∈ R. So, y is divisible by x and z is divisible by y.
So, z is divisible by x ⇒ (x,z) ∈ R
So, R is transitive.
So, R is reflexive and transitive but not symmetric.

(iv)  $R = \{(x, y) : x - y \text{ is an integer}\}$ 

For  $x \in Z$ ,  $(x,x) \notin R$  because x-x=0 is an integer. So, R is reflexive. For,  $x, y \in Z$ , if  $x, y \in R$ , then x-y is an integer  $\Rightarrow (y-x)$  is an integer. So,  $(y,x) \in R$ So, R is symmetric. Let (x, y) and  $(y, z) \in R$ , where  $x, y, z \in Z$ .  $\Rightarrow (x-y)$  and (y-z) are integers.  $\Rightarrow x-z=(x-y)+(y-z)$  is an integer. So, R is transitive.

So, R is reflexive, symmetric and transitive.

(v)

a) R = {(x, y) : x and y work at the same place}
R is reflexive because (x, x) ∈ R
R is symmetric because ,
If (x, y) ∈ R, then x and y work at the same place and y and x also work at the same place. (y, x) ∈ R.
R is transitive because,

Let  $(x, y), (y, z) \in \mathbb{R}$ 

x and  $\mathcal{Y}$  work at the same place and  $\mathcal{Y}$  and z work at the same place.

Then, x and z also works at the same place.  $(x, z) \in R$ . Hence, R is reflexive, symmetric and transitive.

b)  $R = \{(x, y) : x \text{ and } y \text{ live in the same locality} \}$ R is reflexive because  $(x, x) \in R$ R is symmetric because, If  $(x, y) \in R$ , then x and y live in the same locality and y and x also live in the same locality  $(y, x) \in R$ . R is transitive because, Let  $(x, y), (y, z) \in R$ 

x and Y live in the same locality and Y and z live in the same locality.

Then x and z also live in the same locality.  $(x, z) \in R$ . Hence, R is reflexive, symmetric and transitive.

c)  $R = \{(x, y) : x \text{ is exactly 7cm taller than } y\}$ R is not reflexive because  $(x, x) \notin R$ . R is not symmetric because, If  $(x, y) \in R$ , then x is exactly 7cm taller than y and y is clearly not taller than x  $(y, x) \notin R$ . R is not transitive because, Let  $(x, y), (y, z) \in R$ 

x is exactly 7cm taller than Y and Y is exactly 7cm taller than z.

Then x is exactly 14*cm* taller than z.  $(x, z) \notin \mathbb{R}$ Hence, R is neither reflexive nor symmetric nor transitive.

d)  $R = \{(x, y) : x \text{ is wife of } y\}$ 

R is not reflexive because  $(x, x) \notin R$ 

R is not symmetric because,

Let  $(x, y) \in R$ , x is the wife of y and y is not the wife of x.  $(y, x) \notin R$ . R is not transitive because,

```
Let (x, y), (y, z) \in \mathbb{R}
```

x is wife of y and y is wife of z, which is not possible.

 $(x,z) \notin R$ 

Hence, R is neither reflexive nor symmetric nor transitive.

e)  $R = \{(x, y) : x \text{ is father of } y\}$ 

R is not reflexive because  $(x, x) \notin R$ .

R is not symmetric because,

Let  $(x, y) \in R$ , x is the father of y and y is not the father of x.  $(y, x) \notin R$ . R is not transitive because,

Let  $(x, y), (y, z) \in \mathbb{R}$ 

x is father of Y and Y is father of z, x is not father of  $z.(x,z) \notin R$ . Hence, R is neither reflexive nor symmetric nor transitive.

## **Question 2:**

Show that the relation R in the set R of real numbers, defined as  $R = \{(a,b) : a \le b^2\}$  is neither reflexive nor symmetric nor transitive.

## Solution:

 $R = \left\{ (a,b) : a \le b^2 \right\}$  $\left(\frac{1}{2}, \frac{1}{2}\right) \notin R \quad \text{because } \frac{1}{2} > \left(\frac{1}{2}\right)^2$ 

 $\therefore$  R is not reflexive.

 $(1,4) \in R$  as 1 < 4. But 4 is not less than  $1^2$ .  $(4,1) \notin R$ 

 $\therefore$  R is not symmetric.

 $(3,2)(2,1.5) \in R$  [Because  $3 < 2^2 = 4$  and  $2 < (1.5)^2 = 2.25$ ]  $(3,1.5) \notin R$ 

 $\therefore$  R is not transitive.

R is neither reflective nor symmetric nor transitive.

## **Question 3:**

Check whether the relation R defined in the set  $\{1,2,3,4,5,6\}$  as  $R = \{(a,b): b = a+1\}$  is reflexive, symmetric or transitive.

## Solution:

 $A = \{1, 2, 3, 4, 5, 6\}$   $R = \{(a, b) : b = a + 1\}$  $R = \{(1, 2), (2, 3), (3, 4), (4, 5), (5, 6)\}$ 

 $(a,a) \notin R, a \in A$  $(1,1), (2,2), (3,3), (4,4), (5,5) \notin R$  $\therefore$  R is not reflexive.

 $(1,2) \in R$ , but  $(2,1) \notin R$ 

 $\therefore$  R is not symmetric.

 $(1,2),(2,3) \in R$  $(1,3) \notin R$  $\therefore$  R is not transitive.

R is neither reflective nor symmetric nor transitive.

#### **Question 4:**

Show that the relation R in R defined as  $R = \{(a,b): a \le b\}$  is reflexive and transitive, but not symmetric.

#### **Solution:**

 $R = \{(a,b) : a \le b\}$  $(a,a) \in R$  $\therefore \text{ R is reflexive.}$ 

 $(2,4) \in R \text{ (as } 2 < 4)$  $(4,2) \notin R \text{ (as } 4>2)$  $\therefore \text{ R is not symmetric.}$ 

 $(a,b), (b,c) \in R$  $a \le b$  and  $b \le c$  $\Rightarrow a \le c$  $\Rightarrow (a,c) \in R$  $\therefore$  R is transitive.

R is reflexive and transitive but not symmetric.

## **Question 5:**

Check whether the relation R in R defined as  $R = \{(a,b): a \le b^3\}$  is reflexive, symmetric or transitive.

#### **Solution:**

 $R = \left\{ \left(a, b\right) : a \le b^3 \right\}$  $\left(\frac{1}{2}, \frac{1}{2}\right) \notin R, \text{ since } \frac{1}{2} > \left(\frac{1}{2}\right)^3$  $\therefore \text{ R is not reflexive.}$ 

 $(1,2) \in R(as \ 1 < 2^3 = 8)$  $(2,1) \notin R(as \ 2^3 > 1 = 8)$  $\therefore R \text{ is not symmetric.}$ 

$$\left(3,\frac{3}{2}\right), \left(\frac{3}{2},\frac{6}{5}\right) \in R$$
, since  $3 < \left(\frac{3}{2}\right)^3$  and  $\frac{2}{3} < \left(\frac{6}{2}\right)^3$   
 $\left(3,\frac{6}{5}\right) \notin R$   $3 > \left(\frac{6}{5}\right)^3$   
 $\therefore$  R is not transitive.

R is neither reflexive nor symmetric nor transitive.

#### **Question 6:**

Show that the relation R in the set  $\{1,2,3\}$  given by  $R = \{(1,2),(2,1)\}$  is symmetric but neither reflexive nor transitive.

#### **Solution:**

 $A = \{1, 2, 3\}$   $R = \{(1, 2), (2, 1)\}$   $(1, 1), (2, 2), (3, 3) \notin R$   $\therefore \text{ R is not reflexive.}$   $(1, 2) \in R \text{ and } (2, 1) \in R$  $\therefore \text{ R is symmetric.}$ 

 $(1,2) \in R$  and  $(2,1) \in R$  $(1,1) \in R$  $\therefore$  R is not transitive.

R is symmetric, but not reflexive or transitive.

#### **Question 7:**

Show that the relation R in the set A of all books in a library of a college, given by  $R = \{(x, y) : x \text{ and } y \text{ have same number of pages}\}$  is an equivalence relation.

## Solution:

 $R = \{(x, y) : x \text{ and } y \text{ have same number of pages} \}$ 

R is reflexive since  $(x, x) \in R$  as x and x have same number of pages.

 $\therefore$  R is reflexive.

 $(x, y) \in R$ 

*x* and *y* have same number of pages and *y* and *x* have same number of pages  $(y, x) \in R$  $\therefore$  R is symmetric.

 $(x, y) \in R, (y, z) \in R$ 

x and y have same number of pages, y and z have same number of pages. Then x and z have same number of pages.

 $(x,z) \in R$ 

 $\therefore$  R is transitive.

R is an equivalence relation.

## **Question 8:**

Show that the relation R in the set  $A = \{1, 2, 3, 4, 5\}$  given by  $R = \{(a, b) : |a - b| \text{ is even}\}$  is an equivalence relation. Show that all the elements of  $\{1, 3, 5\}$  are related to each other and all the elements of  $\{2, 4\}$  are related to each other. But no element of  $\{1, 3, 5\}$  is related to any element of  $\{2, 4\}$ .

## **Solution:**

 $a \in A$ |a-a| = 0 (which is even)

 $\therefore$  R is reflective.

 $(a,b) \in R$   $\Rightarrow |a-b| \text{ [is even]}$   $\Rightarrow |-(a-b)| = |b-a| \text{ [is even]}$   $(b,a) \in R$  $\therefore$  R is symmetric.

 $(a,b) \in R$  and  $(b,c) \in R$   $\Rightarrow |a-b|_{is \text{ even and }} |b-c|_{is \text{ even}}$   $\Rightarrow (a-b)_{is \text{ even and }} (b-c)_{is \text{ even}}$  $\Rightarrow (a-c) = (a+b) + (b-c)_{is \text{ even}}$   $\Rightarrow |a-b| \text{ is even}$  $\Rightarrow (a,c) \in R$  $\therefore \text{ R is transitive.}$ 

R is an equivalence relation.

All elements of  $\{1,3,5\}$  are related to each other because they are all odd. So, the modulus of the difference between any two elements is even.

Similarly, all elements  $\{2,4\}$  are related to each other because they are all even.

No element of  $\{1,3,5\}$  is related to any elements of  $\{2,4\}$  as all elements of  $\{1,3,5\}$  are odd and all elements of  $\{2,4\}$  are even. So, the modulus of the difference between the two elements will not be even.

## **Question 9:**

Show that each of the relation R in the set  $A = \{x \in \mathbb{Z} : 0 \le x \le 12\}$ , given by

i.  $R = \{(a,b): |a-b| \text{ is a mutiple of } 4\}$ 

ii.  $R = \{(a,b) : a = b\}$ 

Is an equivalence relation. Find the set of all elements related to 1 in each case.

## **Solution:**

$$A = \{x \in Z : 0 \le x \le 12\} = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$$
  
i. 
$$R = \{(a, b) : |a - b| \text{ is a mutiple of } 4\}$$
$$a \in A, (a, a) \in R$$
$$\therefore \text{ R is reflexive.} \qquad [|a - a| = 0 \text{ is a multiple of } 4]$$

 $(a,b) \in R \Rightarrow |a-b|$  [is a multiple of 4]  $\Rightarrow |-(a-b)| = |b-a|$  [is a multiple of 4]  $(b,a) \in R$  $\therefore$  R is symmetric.

$$(a,b) \in R$$
 and  $(b,c) \in R$   
 $\Rightarrow |a-b|$  is a multiple of 4 and  $|b-c|$  is a multiple of 4  
 $\Rightarrow (a-b)$  is a multiple of 4 and  $(b-c)$  is a multiple of 4  
 $\Rightarrow (a-c) = (a-b) + (b-c)$  is a multiple of 4  
 $\Rightarrow |a-c|$  is a multiple of 4

 $\Rightarrow (a,c) \in R$   $\therefore \text{ R is transitive.}$ R is an equivalence relation.

The set of elements related to 1 is  $\{1,5,9\}$  as |1-1| = 0 is a multiple of 4. |5-1| = 4 is a multiple of 4. |9-1| = 8 is a multiple of 4.

ii. 
$$R = \{(a,b) : a = b\}$$
$$a \in A, (a,a) \in R \quad [since a=a]$$
$$\therefore R \text{ is reflective.}$$

$$(a,b) \in R$$
  
 $\Rightarrow a = b$   
 $\Rightarrow b = a$   
 $\Rightarrow (b,a) \in R$   
 $\therefore$  R is symmetric.

$$(a,b) \in R \text{ and } (b,c) \in \mathbb{R}$$
  
 $\Rightarrow a = b \text{ and } b = c$   
 $\Rightarrow a = c$   
 $\Rightarrow (a,c) \in R$   
 $\therefore$  R is transitive.

R is an equivalence relation.

The set of elements related to 1 is  $\{1\}$ .

# **Question 10:**

Give an example of a relation, which is

- i. Symmetric but neither reflexive nor transitive.
- ii. Transitive but neither reflexive nor symmetric.
- iii. Reflexive and symmetric but not transitive.
- iv. Reflexive and transitive but not symmetric.
- v. Symmetric and transitive but not reflexive.

# **Solution:**

i.

$$A = \{5, 6, 7\}$$
  

$$R = \{(5, 6), (6, 5)\}$$
  
(5,5), (6,6), (7,7)  $\notin R$   
R is not reflexive as  $(5,5), (6,6), (7,7) \notin R$   
(5,6), (6,5)  $\in R$  and (6,5)  $\in R$ , R is symmetric.  
 $\Rightarrow (5,6), (6,5) \in R$ , but  $(5,5) \notin R$   
 $\therefore$  R is not transitive.  
Relation R is symmetric but not reflexive or transitive.

ii.  $R = \{(a,b) : a < b\}$ 

 $a \in R, (a, a) \notin R$  [since *a* cannot be less than itself] R is not reflexive.  $(1,2) \in R(as 1 < 2)$ But 2 is not less than 1  $\therefore (2,1) \notin R$ R is not symmetric.  $(a,b), (b,c) \in R$   $\Rightarrow a < b$  and b < c  $\Rightarrow a < c$  $\Rightarrow (a,c) \in R$ 

 $\therefore$  R is transitive.

Relation R is transitive but not reflexive and symmetric.

iii.  $A = \{4, 6, 8\}$  $A = \{(4, 4), (6, 6), (8, 8), (4, 6), (6, 8), (8, 6)\}$ 

R is reflexive since  $a \in A, (a, a) \in R$ 

*R* is symmetric since  $(a, b) \in R$ 

$$\Rightarrow (b,a) \in R \quad for a, b \in R$$

*R* is not transitive since  $(4,6), (6,8) \in R, but (4,8) \notin R$ R is reflexive and symmetric but not transitive.

iv. 
$$R = \{(a,b) : a^3 > b^3\}$$
$$(a,a) \in R$$
$$\therefore \text{ R is reflexive.}$$
$$(2,1) \in R$$
$$But(1,2) \notin R$$

 $\therefore$  R is not symmetric.

$$(a,b),(b,c) \in R$$
  
 $\Rightarrow a^3 \ge b^3 \text{ and } b^3 < c^3$   
 $\Rightarrow a^3 < c^3$   
 $\Rightarrow (a,c) \in R$   
 $\therefore R$  is transitive.  
R is reflexive and transitive but not symmetric

v. Let 
$$A = \{-5, -6\}$$
  
 $R = \{(-5, -6), (-6, -5), (-5, -5)\}$   
R is not reflexive as  $(-6, -6) \notin R$   
 $(-5, -6), (-6, -5) \in R$   
R is symmetric.  
 $(-5, -6), (-6, -5) \in R$   
 $(-5, -5) \in R$   
R is transitive.  
 $\therefore$  R is symmetric and transitive but not reflexive.

## **Question 11:**

Show that the relation R in the set A of points in a plane given by

 $R = \{(P,Q) : \text{Distance of the point P from the origin is same as the distance of the point Q from the origin}\}$ 

, is an equivalence relation. Further, show that the set of all points related to a point  $P \neq (0,0)$  is the circle passing through P with origin as centre.

## Solution:

 $R = \{(P,Q) : \text{Distance of the point P from the origin is same as the distance of the point Q from the origin}\}$ 

Clearly,  $(P, P) \in R$   $\therefore$  R is reflexive.  $(P,Q) \in R$ Clearly R is symmetric.  $(P,Q), (Q,S) \in R$  $\Rightarrow$  The distance of P and

 $\Rightarrow$  The distance of *P* and *Q* from the origin is the same and also, the distance of *Q* and *S* from the origin is the same.

 $\Rightarrow$  The distance of *P* and *S* from the origin is the same.

 $(P,S) \in R$ 

 $\therefore$  R is transitive.

R is an equivalence relation.

The set of points related to  $P \neq (0,0)$  will be those points whose distance from origin is same as distance of P from the origin.

Set of points forms a circle with the centre as origin and this circle passes through P.

## **Question 12:**

Show that the relation R in the set A of all triangles as  $R = \{(T_1, T_2): T_1 \text{ is similar to } T_2\}$ , is an equivalence relation. Consider three right angle triangles  $T_1$  with sides 3,4,5,  $T_2$  with sides 5,12,13 and  $T_3$  with sides 6,8,10. Which triangle among  $T_1, T_2, T_3$  are related?

## **Solution:**

 $R = \{(T_1, T_2) : T_1 \text{ is similar to } T_2\}$ R is reflexive since every triangle is similar to itself.

If  $(T_1, T_2) \in R$ , then  $T_1$  is similar to  $T_2$ .  $T_2$  is similar to  $T_1$ .  $\Rightarrow (T_2, T_1) \in R$  $\therefore$  R is symmetric.

 $(T_1,T_2),(T_2,T_3) \in \mathbb{R}$ 

 $T_1$  is similar to  $T_2$  and  $T_2$  is similar to  $T_3$ .

 $\therefore T_{1 \text{ is similar to }} T_{3}.$   $\Rightarrow (T_{1}, T_{3}) \in R$   $\therefore \text{ R is transitive.}$  $\frac{3}{6} = \frac{4}{8} = \frac{5}{10} = \left(\frac{1}{2}\right)$ 

 $\therefore$  Corresponding sides of triangles  $T_1$  and  $T_3$  are in the same ratio. Triangle  $T_1$  is similar to triangle  $T_3$ . Hence,  $T_1$  is related to  $T_3$ .

# **Question 13:**

Show that the relation R in the set A of all polygons as  $R = \{(P_1, P_2) : P_1 \text{ and } P_2 \text{ have same number of sides}\}$ , is an equivalence relation. What is the set of all elements in A related to the right angle triangle T with sides 3,4*and*5?

## Solution:

 $R = \{(P_1, P_2) : P_1 \text{ and } P_2 \text{ have same number of sides}\}$  $(P_1, P_2) \in R \text{ as same polygon has same number of sides.}$  $\therefore \text{ R is reflexive.}$  $(P_1, P_2) \in R$  $\Rightarrow P_1 \text{ and } P_2 \text{ have same number of sides.}$  $\Rightarrow P_2 \text{ and } P_1 \text{ have same number of sides.}$  $\Rightarrow (P_2, P_1) \in R$  $\therefore \text{ R is symmetric.}$ 

 $(P_1, P_2), (P_2, P_3) \in R$   $\Rightarrow P_1$  and  $P_2$  have same number of sides.  $P_2$  and  $P_3$  have same number of sides.  $\Rightarrow P_1$  and  $P_3$  have same number of sides.  $\Rightarrow (P_1, P_3) \in R$   $\therefore$  R is transitive. R is an equivalence relation.

The elements in A related to right-angled triangle (T) with sides 3,4,5 are those polygons which have three sides.

Set of all elements in a related to triangle T is the set of all triangles.

# **Question 14:**

Let L be the set of all lines in XY plane and R be the relation in L defined as  $R = \{(L_1, L_2) : L_1 \text{ is parallel to } L_2\}$ . Show that R is an equivalence relation. Find the set of all lines related to the line y = 2x + 4.

# Solution:

 $R = \{(L_1, L_2) : L_1 \text{ is parallel to } L_2\}$ R is reflexive as any line  $L_1$  is parallel to itself i.e.,  $(L_1, L_2) \in R$ If  $(L_1, L_2) \in R$ , then  $\Rightarrow L_1$  is parallel to  $L_2$ .  $\Rightarrow L_2$  is parallel to  $L_1$ .  $\Rightarrow (L_2, L_1) \in R$  $\therefore$  R is symmetric.

 $(L_1, L_2), (L_2, L_3) \in R$   $\Rightarrow L_1$  is parallel to  $L_2$   $\Rightarrow L_2$  is parallel to  $L_3$   $\therefore L_1$  is parallel to  $L_3$ .  $\Rightarrow (L_1, L_3) \in R$  $\therefore \mathbb{R}$  is transitive.

R is an equivalence relation.

Set of all lines related to the line y = 2x + 4 is the set of all lines that are parallel to the line y = 2x + 4.

Slope of the line y = 2x + 4 is m = 2.

Line parallel to the given line is in the form y = 2x + c, where  $c \in R$ .

Set of all lines related to the given line is given by y = 2x + c, where  $c \in R$ . Question 15:

Let R be the relation in the set  $\{1,2,3,4\}$  given by

 $R = \{(1,2)(2,2), (1,1), (4,4), (1,3), (3,3), (3,2)\}$ 

Choose the correct answer.

- A. R is reflexive and symmetric but not transitive.
- B. R is reflexive and transitive but not symmetric.
- C. R is symmetric and transitive but not reflexive.
- D. R is an equivalence relation.

#### Solution:

 $R = \{(1,2)(2,2), (1,1), (4,4), (1,3), (3,3), (3,2)\}$ (*a*,*a*)  $\in R$  for every  $a \in \{1,2,3,4\}$  $\therefore$  R is reflexive.

 $(1,2) \in R$  but  $(2,1) \notin R$  $\therefore$  R is not symmetric.

 $(a,b), (b,c) \in R$  for all  $a, b, c \in \{1,2,3,4\}$  $\therefore$  R is not transitive.

R is reflexive and transitive but not symmetric.

The correct answer is B.

**Question 16:** 

Let R be the relation in the set N given by  $R = \{(a,b): a = b - 2, b > 6\}$ . Choose the correct answer.

A.  $(2,4) \in R$ B.  $(3,8) \in R$ C.  $(6,8) \in R$ D.  $(8,7) \in R$ 

# Solution:

 $R = \{(a,b): a = b - 2, b > 6\}$ Now,  $b > 6, (2,4) \notin R$  $3 \neq 8 - 2$  $\therefore (3,8) \notin R \text{ and as } 8 \neq 7 - 2$  $\therefore (8,7) \notin R$ Consider (6,8) 8 > 6 and 6 = 8 - 2 $\therefore (6,8) \in R$ The correct answer is C.