<u>Two charges $5 \times 10^{-8}C$ and $-3 \times 10^{-8}C$ are located 16 cm apart. At what point(s) on</u> the line joining the two charges is the electric potential zero? Take the potential at infinity to be zero.

Answer:

Given, two charge particles

$$q_1 = 5 * 10^{-8}C$$

 $q_2 = -3 * 10^{-8}C$

The separation between two charged particle $d = 16c_m = 0.16m$

Now, let's assume the point P between two charged particles where the electric potential is zero is x meter away from q_1 and (9 - x) meter away from q_2

So,

The potential at point P:

$$V_p = \frac{kq_1}{x} + \frac{kq_2}{0.16 - x} = 0$$
$$V_p = \frac{k5 * 10^{-8}}{x} + \frac{k(-3 * 10^{-8})}{0.16 - x} = 0$$
$$\frac{k5 * 10^{-8}}{x} = -\frac{k(-3 * 10^{-8})}{0.16 - x}$$

5(0.16 - x) = 3x

x = 0.1m = 10cm

Hence the point between two charged particles where the electric potential is zero lies 10cm away from q_1 and 6 cm away from q_2

Now, Let's assume a point Q which is outside the line segment joining two charges and having zero electric potential .let the point Q lie r meter away from q_2 and (0.16+r) meter away from q_1

So electric potential at point Q = 0

$$\frac{kq_1}{0.16+r} + \frac{kq_2}{r} = 0$$
$$\frac{k5*10^{-8}}{0.16+r} + \frac{k(-3*10^{-8})}{r} = 0$$

$$5r = 3(0.16 + r)$$

r = 0.24m = 24cm

Hence the second point where the electric potential is zero is 24cm away from q_2 and 40cm away from q_1

2.2 <u>A regular hexagon of side 10 cm has a charge $5\mu C$ at each of its vertices. Calculate</u> the potential at the centre of the hexagon.

Answer:



The electric potential at O due to one charge,

$$V_1 = \frac{q}{4\pi\epsilon_0 r}$$

 $q = 5 \times 10^{-6} C$

r = distance between charge and O = 10 cm = 0.1 m

direction to the total electric potential at the point O.

$$V = 6 \times \frac{q}{4\pi\epsilon_0 r}$$

$$\implies V = 6 \times \frac{9 \times 10^9 N m^2 C^{-2} \times 5 \times 10^{-6} C}{0.1m}$$

= $2.7 \times 10^6 V$

Therefore the required potential at the centre is $2.7\times 10^6 V$

2.3 (a) <u>Two charges ${}^{2\mu C}$ and ${}^{-2\mu C}$ are placed at points A and B 6 cm apart. (a) Identify an equipotential surface of the system.</u>

Answer:

Given, 2 charges with charges $^{2\mu C}$ and $^{-2\mu C}$.

An equipotential plane is a plane where the electric potential is the same at every point on the plane. Here if we see the plane which is perpendicular to line AB and passes through the midpoint of the line segment joining A and B, we see that at every point the electric potential is zero because the distance of all the points from two charged particles is same. Since the magnitude of charges is the same they cancel out the electric potential by them.

Hence required plane is plane perpendicular to line AB and passing through the midpoint of AB which is 3cm away from both charges.

2.3 (b) <u>Two charges ${}^{2\mu C}$ and ${}^{-2\mu C}$ are placed at points A and B 6 cm apart. (b) What is the direction of the electric field at every point on this surface?</u>

Answer:

The direction of the electric field in this surface is normal to the plane and in the direction of line joining A and B. Since both charges have the same magnitude and different sign, they cancel out the component of the electric field which is parallel to the surface.

2.4 (a) <u>A spherical conductor of radius 12 cm has a charge of $1.6 \times 10^{-7} C$ distributed uniformly on its surface. What is the electric field (a) inside the sphere</u>

Answer:

Since the charge is uniformly distributed and it always remains on the surface of the conductor, the electric field inside the sphere will be zero.

2.4 (b) <u>A spherical conductor of radius 12 cm has a charge of $1.6 \times 10^{-7}C$ distributed uniformly on its surface. What is the electric field(b) just outside the sphere</u>

Answer:

Given,

Charge on the conductor $q=1.6\ast 10^{-7}C$

The radius of a spherical conductor R = 12cm = 0.12m

Now,

the electric field outside the spherical conductor is given by:

$$E = \frac{kq}{r^2} = \frac{1}{4\pi\epsilon} \frac{q}{r^2} = \frac{9*10^9*1.6*10^{-7}}{0.12^2} = 10^5 NC^{-1}$$

Hence electric field just outside is $10^5 NC^{-1}$

2.4 (c) <u>A spherical conductor of radius 12 cm has a charge of $1.6 \times 10^{-7}C$ distributed uniformly on its surface. What is the electric field (c) at a point 18 cm from the centre of the sphere?</u>

Answer:

Given,

charge on the conductor $q = 1.6 \ast 10^{-7} C$

The radius of the spherical conductor R = 12cm = 0.12m

Now,

the electric field at point 18cm away from the centre of the spherical conductor is given by:

$$E = \frac{kq}{r^2} = \frac{1}{4\pi\epsilon} \frac{q}{r^2} = \frac{9*10^9*1.6*10^{-7}}{0.18^2} = 4.4*10^4 NC^{-1}$$

Hence electric field at the point 18cm away from the centre of the sphere is $4.4 \ast 10^4 NC^{-1}$

2.5 <u>A parallel plate capacitor with air between the plates has a capacitance of 8</u> $pF(1pF = 10^{-12}F)$. What will be the capacitance if the distance between the plates is reduced by half, and the space between them is filled with a substance of dielectric constant 6?

Answer:

As we know,

$$C = \frac{\epsilon_r \epsilon_0 A}{d}$$

where A= area of the plate

 ϵ_0 = permittivity of the free space

d = distance between the plates.

Now, Given

The capacitance between plates initially

$$C_{initial} = 8pF = \frac{\epsilon A}{d}$$

Now, capacitance when the distance is reduced half and filled with the substance of dielectric 6

$$C_{final} = \frac{6\epsilon_0 A}{d/2} = 12 \frac{\epsilon_0 A}{d} = 12 * 8pF = 96pF$$

Hence new capacitance is 96pF.

2.6 (a) <u>Three capacitors each of capacitance 9 pF are connected in series. (a) What is</u> <u>the total capacitance of the combination?</u>

Answer:

Given, 3 capacitor of 9pF connected in series,

the equivalent capacitance when connected in series is given by

$$\frac{1}{C_{equivalent}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$
$$\frac{1}{C_{equivalent}} = \frac{1}{9} + \frac{1}{9} + \frac{1}{9} = \frac{3}{9} = \frac{1}{3}$$
$$C_{equivalent} = 3pF$$

Hence total capacitance of the combination is 3pF

2.6 (b) <u>Three capacitors each of capacitance 9 pF are connected in series. (b) What is</u> <u>the potential difference across each capacitor if the combination is connected to a 120 V</u> <u>supply?</u>

Answer:

Given,

supply Voltage V = 120 V

The potential difference across each capacitor will be one-third of the total voltage

$$V_c = \frac{V}{3} = \frac{120}{3} = 40V$$

Hence potential difference across each capacitor is 40V.

2.7 (a) <u>Three capacitors of capacitances 2 pF, 3 pF and 4 pF are connected in parallel.</u> (a) What is the total capacitance of the combination?

Answer:

Given, 3 capacitors with $C_1 = 2pF, C_2 = 3pFandC_3 = 4pF$ are connected in series,

the equivalent capacitance when connected in parallel is given by

$$C_{equivalant} = C_1 + C_2 + C_3$$

$$C_{equivalant} = 2 + 3 + 4 = 9pF$$

Hence, the equivalent capacitance is 9pF.

2.7 (b) <u>Three capacitors of capacitances 2 pF, 3 pF and 4 pF are connected in parallel.</u> (b) Determine the charge on each capacitor if the combination is connected to a 100 V <u>supply.</u>

Answer:

Given, 3 capacitors connected in parallel with

 $C_1 = 2pF$

$$C_2 = 3pF$$

 $C_3 = 4pF$

Supply voltage V = 100V

Since they are connected in parallel, the voltage across each capacitor is 100V.

So, charge on 2pf capacitor :

$$Q_1 = C_1 V = 2 * 10^{-12} * 100 = 2 * 10^{-10} C$$

Charge on 3pF capacitor:

$$Q_2 = C_2 V = 3 * 10^{-12} * 100 = 3 * 10^{-10} C$$

Charge on 4pF capacitor:

$$Q_3 = C_3 V = 4 * 10^{-12} * 100 = 4 * 10^{-10} C_3$$

Hence charges on capacitors are 2pC,3pC and 4pC respectively

2.8 In a parallel plate capacitor with air between the plates, each plate has an area of $6 \times 10^{-3} m^2$ and the distance between the plates is 3 mm. Calculate the capacitance of the capacitor. If this capacitor is connected to a 100 V supply, what is the charge on each plate of the capacitor?

Answer:

Given,

Area of the capacitor plate $A = 6 \times 10^{-3} m^2$

Distance between the plates d = 3mm

Now,

The capacitance of the parallel plate capacitor is

$$C = \frac{\epsilon_0 A}{d}$$

 ϵ_0 = permittivity of free space = $8.854 * 10^{-12} N^{-1} m^{-2} C^2$

putting all know value we get,

$$C = \frac{8.854 * 10^{-12} * 6 * 10^{-3}}{3 * 10^{-3}} = 17.71 * 10^{-12} F = 17.71 pF$$

Hence capacitance of the capacitor is 17.71pF.

Now,

Charge on the plate of the capacitor :

$$Q = CV = 17.71 * 10^{-12} * 100 = 1.771 * 10^{-9}C$$

Hence charge on each plate of the capacitor is $1.771 * 10^{-9}C$.

2.9 (a) Explain what would happen if in the capacitor given in exercise 2.8, a 3 mm thick mica sheet (of dielectric constant = 6) were inserted between the plates, (a) while the voltage supply remained connected.

Answer:

Given,

The dielectric constant of the inserted mica sheet = 6

The thickness of the sheet = 3mm

Supply voltage V = 100V

Initial capacitance = $C_{initial} = 1.771 * 10^{-11} F$

Final capacitance = $KC_{initial} = 6 * 1.771 * 10^{-11} F = 106 * 10^{-12} F$

Final charge on the capacitor = $Q_{final} = C_{final}V = 106 * 10^{-12} * 100 = 106 * 10^{-10}C$

Hence on inserting the sheet charge on each plate changes to $106*10^{-10}C$.

2.9 (b) Explain what would happen if in the capacitor given, a 3 mm thick mica sheet (of dielectric constant = 6) were inserted between the plates,(b) after the supply was disconnected.

Answer:

If a 3mm mica sheet is inserted between plates of the capacitor after disconnecting it from the power supply, the voltage across the capacitor be changed. Since the charge on the capacitor can not go anywhere, if we change the capacitance (which we are doing by inserting mica sheet here), the voltage across the capacitor has to be adjusted accordingly.

As obtained from question number 8 charge on each plate of the capacitor is $1.771 \ast 10^{-9} C$

$$V_{final} = \frac{Q}{C_{final}} = \frac{1.771 \times 10^{-9}}{106 \times 10^{-12}} = 16.7V$$

2.10 <u>A 12pF capacitor is connected to a 50V battery. How much electrostatic energy is</u> stored in the capacitor?

Answer:

As we know,

the electrostatic energy stored in the capacitor is

 $E=\frac{1}{2}CV^2$

Here,

$$C = 12pF$$

$$V = 50V$$

So,

$$E = \frac{1}{2}CV^2 = \frac{1}{2}12 * 10^{-12} * 50^2 = 1.5 * 10^{-8}J$$

Hence energy stored in the capacitor is $1.5 * 10^{-8} J$

2.11 <u>A 600pF capacitor is charged by a 200V supply. It is then disconnected from the</u> supply and is connected to another uncharged 600 pF capacitor. How much electrostatic energy is lost in the process?

Answer:

Given

C = 600 pF

$$V = 200V$$

Energy stored :

$$E = \frac{1}{2}CV^2 = \frac{1}{2} * 600 * 10^{-12} * 200 * 200 = 1.2 * 10^{-5}J$$

Now, when it is disconnected and connected from another capacitor of capacitance 600pF

New capacitance

$$C' = \frac{600 * 600}{600 + 600} = 300 pF$$

New electrostatic energy

$$E' = \frac{1}{2}C'V^2 = \frac{1}{2} * 300 * 10^{-12} * 200^2 = 0.6 * 10^{-5}J$$

Hence loss in energy

$$E - E' = 1.2 * 10^{-5} - 0.6 * 10^{-5} J = 0.6 * 10^{-5}$$

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NCERT solutions for class 12 physics chapter 2 electrostatic potential and capacitance additional exercises:

2.12 <u>A charge of 8 mC is located at the origin. Calculate the work done in taking a small</u> <u>charge of $-2 \times 10^{-9}C$ from a point P (0, 0, 3 cm) to a point Q (0, 4 cm, 0), via a point</u> <u>R (0, 6 cm, 9 cm).</u>

Answer:

Given,

The initial distance between two charges

 $d_{initial} = 3cm$

The final distance between two charges

 $d_{final} = 4cm$

Hence total work is done

$$W = 9 * 10^9 * 8 * 10^{-3} * (-2 * 10^{-9}) \left(\frac{1}{0.04} - \frac{1}{0.03}\right) = 1.27J$$

The path of the charge does not matter, only initial and final position matters.

2.13 <u>A cube of side b has a charge q at each of its vertices. Determine the potential and</u> electric field due to this charge array at the centre of the cube.

Answer:

As we know,

the distance between vertices and the centre of the cube

$$d = \frac{\sqrt{3}b}{2}$$

Where b is the side of the cube.

So potential at the centre of the cube:

$$P = 8 * \frac{kq}{d} = 8 * \frac{kq}{b\sqrt{3}/2} = \frac{16kq}{b\sqrt{3}}$$

Hence electric potential at the centre will be

$$\frac{16kq}{b\sqrt{3}} = \frac{16q}{4\pi\epsilon_0 b\sqrt{3}} = \frac{4q}{\pi\epsilon_0 b\sqrt{3}}$$

The electric field will be zero at the centre due to symmetry i.e. every charge lying in the opposite vertices will cancel each other's field.

2.14 (a) <u>Two tiny spheres carrying charges $1.5\mu C$ and $2.5\mu C$ are located 30 cm apart.</u> <u>Find the potential and electric field:</u>

(a) at the mid-point of the line joining the two charges

Answer:

As we know

outside the sphere, we can assume it like a point charge. so,

the electric potential at midpoint of the two-sphere

$$V = \frac{kq_1}{d/2} + \frac{kq_2}{d/2}$$

where q1 and q2 are charges and d is the distance between them

So,

$$V = \frac{k1.5 * 10^{-6}}{0.15} + \frac{k2.5 * 10^{-6}}{0.15} = 2.4 * 10^5 V$$

The electric field

$$E = \frac{k1.5 * 10^{-6}}{0.15^2} - \frac{k2.5 * 10^{-6}}{0.15^2} = 4 * 10^5 V/m$$

2.14 (b) <u>Two tiny spheres carrying charges $1.5\mu C$ and $2.5\mu C$ are located 30 cm apart.</u> Find the potential and electric field:

(b) at a point 10 cm from this midpoint in a plane normal to the line and passing through the mid-point.

Answer:

The distance of the point from both the charges :

$$d = \sqrt{0.1^2 + 0.15^2} = 0.18m$$

Hence,

Electric potential:

$$V = \frac{kq_1}{d} + \frac{kq_2}{d} = \frac{k}{0.18}(1.5 + 2.5) * 10^{-6} = 2 * 10^5 V$$

Electric field due to q1

$$E_1 = \frac{kq_1}{d^2} = \frac{k1.5\mu C}{0.18^2 m^2} = 0.416 * 10^6 V/m$$

Electric field due to q2

$$E_2 = \frac{kq_2}{d^2} = \frac{k2.5\mu C}{0.18^2 m^2} = 0.69 * 10^6 V/m$$

Now,

Resultant Electric field :

$$E = \sqrt{E_1^2 + E_2^2 + 2E_1E_2\cos\theta}$$

Where θ is the angle between both electric field directions

Here,

$$cos\frac{\theta}{2} = \frac{0.10}{0.18} = \frac{5}{9}$$

 $\frac{\theta}{2} = 56.25$

 $\theta = 2 * 56.25 = 112.5$

Hence

$$E = \sqrt{(0.416 * 10^6)^2 + (0.69 * 10^6)^2 + 2(0.416 * 10^6)(0.69 * 10^6)cos112.5}$$

 $E=6.6*\,10^5 V/m$

2.15 (a) <u>A spherical conducting shell of inner radius r $_1$ and outer radius r $_2$ has a charge <u>Q</u>.</u>

(a) A charge q is placed at the centre of the shell. What is the surface charge density on the inner and outer surfaces of the shell?

Answer:

The charge placed on the centre is q, so -q will be the charge induced in the inner shell and + q will be induced in the outer shell

So,

charge density on the inner shell

 $\sigma_{inner} = \frac{-q}{4\pi r_1^2}$

charge Density on the outer shell

 $\sigma_{outer} = \frac{Q+q}{4\pi r_2^2}$

2.15 (b) <u>A spherical conducting shell of inner radius r₁ and outer radius r₂ has a charge Q.</u>

(b)Is the electric field inside a cavity (with no charge) zero, even if the shell is not spherical, but has any irregular shape? Explain.

Answer:

Yes, the electric field inside the cavity is zero even when the shape is irregular and not the sphere. Suppose a Gaussian surface inside the cavity, now since there is no charge inside it, the electric flux through it will be zero according to the guess law. Also, all of the charges will reside on the surface of the conductor so, net charge inside is zero. hence electric field inside cavity is zero.

2.16 (a) Show that the normal component of the electrostatic field has a discontinuity $(E_1 - E_2).\hat{n} = \frac{\sigma}{\epsilon_0}$ from one side of a charged surface to another given by

where n^ is a unit vector normal to the surface at a point and σ is the surface charge density at that point. Hence, show that just outside a conductor, the electric field is $\sigma \frac{\widehat{n}}{\epsilon_0}$

Answer:

The electric field on one side of Surface with charge density σ

$$E_1 = -\frac{\sigma}{2\epsilon_0}\widehat{n}$$

The electric field on another side of Surface with charge density σ

$$E_2 = -\frac{\sigma}{2\epsilon_0}\widehat{n}$$

Now, resultant of both surfaces:

As E1 and E2 are opposite in direction. we have

$$E_1 - E_2 = \frac{\sigma}{2\epsilon_0} - \left(-\frac{\sigma}{2\epsilon_0}\right)\widehat{n} = \frac{\sigma}{\epsilon_0}$$

There has to be a discontinuity at the sheet of the charge since both electric fields are in the opposite direction.

Now,

Since the electric field is zero inside the conductor,

the electric field just outside the conductor is

$$E = \frac{\sigma}{\epsilon_0} \hat{n}$$

2.16 (b) <u>Show that the tangential component of electrostatic field is continuous from one</u> <u>side of a charged surface to another. [Hint: For (a), use Gauss's law. For, (b) use the</u> <u>fact that work done by electrostatic field on a closed loop is zero.]</u>

Answer:

Let's assume a rectangular loop of length I and small width b.

Now,

Line integral along the loop :

$$\oint E.dl = E_1 l - E_2 l = 0$$

This implies

$$E_1 \cos\theta_1 l - E_2 \cos\theta_2 l = 0$$

From here,

 $E_1 cos\theta_1 = E_2 cos\theta_2$

Since $E_1 cos\theta_1$ and $E_2 cos\theta_2$ are the tangential component of the electric field, the tangential component of the electric field is continuous across the surface

2.17 <u>A long charged cylinder of linear charged density λ is surrounded by a hollow coaxial conducting cylinder. What is the electric field in the space between the two cylinders?</u>

Answer:

The charge density of the cylinder with length I and radius r = λ

The radius of another hollow cylinder with same length = R

Now, let our gaussian surface be a cylinder with the same length and different radius r

the electric flux through Gaussian surface

$$\oint E.ds = \frac{q}{\epsilon_0}$$
$$E.2\pi r l = \frac{\lambda l}{\epsilon_0}$$
$$E. = \frac{\lambda}{2\pi\epsilon_0 r}$$

Hence electric field ar a distance r from the axis of the cylinder is

$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

2.18 (a) In a hydrogen atom, the electron and proton are bound at a distance of <u>about 0.53</u> A

(a) Estimate the potential energy of the system in eV, taking the zero of the potential energy at an infinite separation of the electron from proton

Answer:

As we know,

the distance between electron-proton of the hydrogen atom

 $d = 0.53 * 10^{-10} m$

The potential energy of the system = potential energy at infinity - potential energy at distance d

$$PE = 0 - \frac{ke * e}{d} = -\frac{9 * 10^9 (1.6 * 10^{-19})^2}{0.53 * 10^{10}} = -43.7 * 10^{-19} J$$

As we know,

$$1ev = 1.6 * 10^{-19} J$$
$$PE = \frac{-43.7 * 10^{-19}}{1.6 * 10^{-19}} = -27.2eV$$

Hence potential energy of the system is -27.2eV.

2.18 (b) In a hydrogen atom, the electron and proton are bound at a distance of about 0.53 Å

(b) What is the minimum work required to free the electron, given that its kinetic energy in the orbit is half the magnitude of potential energy obtained in (a)?

Answer:

the potential energy of the system is -27.2eV. (from the previous question)

Kinetic energy is half of the potential energy in magnitude. so kinetic energy = 27/2 = 13.6eV

SO,

total energy = 13.6 - 27.2 = -13.6eV

Hence the minimum work required to free the electron is 13.6eV

2.18 (c) In a hydrogen atom, the electron and proton are bound at a distance of about $0.53 \dot{A}$:

(c) What are the answers to (a) and (b) above if the zero of potential energy is taken at <u>1.06</u> Åseparation?

Answer:

When potential energy is zero at d' 1.06 \dot{A} away,

The potential energy of the system =potential energy at d' -potential energy at d

$$PE = \frac{ke * p}{d_1} - 27.2 = \frac{9 * 10^9 * (1.6 * 10^{-19})^2}{1.06 * 10^{-10}} = -13.6eV$$

Hence potential energy, in this case, would be -13.6eV

2.19 If one of the two electrons of a H $_2$ molecule is removed, we get a hydrogen molecular ion H_2^+ . In the ground state of an H_2^+ , the two protons are separated by roughly 1.5 \dot{A} , and the electron is roughly 1 \dot{A} from each proton. Determine the potential energy of the system. Specify your choice of the zero of potential energy.

Answer:

Given,

Distance between proton 1 and 2

$$d_{p_1 - p_2} = 1.5 * 10^{-10} m$$

Distance between proton 1 and electron

$$d_{p_1-e} = 1 * 10^{-10} m$$

Distance between proton 2 and electron

$$d_{p_2-e} = 1 * 10^{-10} m$$

Now,

The potential energy of the system :

$$V = \frac{kp_1e}{d_{p_1-e}} + \frac{kp_2e}{d_{p_2-e}} + \frac{kp_1p_2}{d_{p_1-p_2}}$$

Substituting the values, we get

$$V = \frac{9 * 10^9 * 10^{-19} * 10^{-19}}{10^{-10}} \left[-(16)^2 + \frac{(1.6)^2}{1.5} - (1.6)^2 \right] = -19.2eV$$

2.20 <u>Two charged conducting spheres of radii a and b are connected to each other by a</u> wire. What is the ratio of electric fields at the surfaces of the two spheres? Use the result obtained to explain why charge density on the sharp and pointed ends of a conductor is higher than on its flatter portions.

Answer:

Since both spheres are connected through the wire, their potential will be the same

Let electric field at A and B be $E_A and E_B$.

Now,

$$\frac{E_A}{E_B} = \frac{Q_A}{Q_B} * \frac{b^2}{a^2}$$

also

$$\frac{Q_A}{Q_B} = \frac{C_a V}{C_B V}$$

Also

$$\frac{C_A}{C_B} = \frac{a}{b}$$

Therefore,

 $\frac{E_A}{E_B} = \frac{ab^2}{ba^2} = \frac{b}{a}$

Therefore the ratio of the electric field is b/a.

2.21 (a) <u>Two charges –q and +q are located at points (0, 0, –a) and (0, 0, a),</u> respectively.

(a) What is the electrostatic potential at the points (0, 0, z) and (x, y, 0)?

Answer:

1)electric potential at point (0,0,z)

distance from q_1

 $d_1 = \sqrt{0^2 + 0^2 + (0 - a - z)^2} = a + z$

distance from q_2

$$d_2 = \sqrt{0^2 + 0^2 + (a - z)^2} = a - z$$

Now,

Electric potential :

$$V = \frac{kq_1}{a+z} + \frac{kq_2}{a-z} = \frac{2kqa}{z^2 - a^2}$$

2) Since the point,(x,y,0) lies in the normal to the axis of the dipole, the electric potential at this point is zero.

2.21 (b) <u>Two charges –q and +q are located at points (0, 0, –a) and (0, 0, a),</u> respectively.

(b) Obtain the dependence of potential on the distance r of a point from the origin $\frac{r}{a} >> 1$ when $\frac{r}{a} >> 1$

Answer:

Here, since distance r is much greater than half the distance between charges, the potential V at a distance r is inversely proportional to the square of the distance

$$V \propto \frac{1}{r^2}$$

2.21 (c) <u>Two charges –q and +q are located at points (0, 0, –a) and (0, 0, a),</u> respectively

(c) How much work is done in moving a small test charge from the point (5,0,0) to (– 7,0,0) along the x-axis? Does the answer change if the path of the test charge between the same points is not along the x-axis?

Answer:

Since point (5,0,0) is equidistance from both charges, they both will cancel out each other potential and hence potential at this point is zero.

Similarly, point (–7,0,0) is also equidistance from both charges. and hence potential at this point is zero.

Since potential at both the point is zero, the work done in moving charge from one point to other is zero. Work done is independent of the path.

2.22 Figure shows a charge array known as an electric quadrupole. For a point on the axis of the quadrupole, obtain the dependence of potential on r for $a^{r} >> 1$, and contrast your results with that due to an electric dipole, and an electric monopole (i.e., a single charge).

Answer:

Here, As we can see

The electrostatic potential caused by the system of three charges at point P is given by

$$V = \frac{1}{4\pi\varepsilon_0} \left[\frac{q}{r+a} - \frac{2q}{r} + \frac{q}{r-a} \right]$$

$$V = \frac{q}{4\pi\epsilon_0} \left[\frac{2a^2}{r^3(1-\frac{a^2}{r^2})} \right]$$

Since

 $\frac{r}{a} >> 1$

$$V = \frac{2qa^2}{4\pi\epsilon_0 r^3}$$

From here we conclude that

$$V \propto \frac{1}{r^3}$$

Whereas we know that for a dipole,

$$V \propto \frac{1}{r^2}$$

And for a monopole,

$$V \propto \frac{1}{r}$$

2.23 <u>An electrical technician requires a capacitance of $2\mu F$ in a circuit across a</u> potential difference of 1 kV. A large number of $1\mu F$ capacitors are available to him each of which can withstand a potential difference of not more than 400 V. Suggest a possible arrangement that requires the minimum number of capacitors

Answer:

Let's assume n capacitor connected in series and m number of such rows,

Now,

As given

The total voltage of the circuit = 1000V

and the total voltage a capacitor can withstand = 400

From here the total number of the capacitor in series

$$n = \frac{1000}{400} = 2.5$$

Since the number of capacitors can never be a fraction, we take n = 3.

Now,

Total capacitance required = $2\mu F$

Number of rows we need

m = 2 * n = 2 * 3 = 6

Hence capacitors should be connected in 6 parallel rows where each row contains 3 capacitors in series.

2.24 <u>What is the area of the plates of a 2 F parallel plate capacitor, given that the</u> <u>separation between the plates is 0.5 cm?</u> [You will realise from your answer why <u>ordinary capacitors are in the range of μF or less. However, electrolytic capacitors do</u> <u>have a much larger capacitance (0.1 F) because of very minute separation between the</u> <u>conductors.]</u>

Answer:

Given,

The capacitance of the parallel plate capacitor ${\cal C}=2F$

Separation between plated d = 0.5cm

Now, As we know

 $C = \frac{\epsilon_0 A}{d}$

$$A = \frac{Cd}{\epsilon_0} = \frac{2*5*10^{-3}}{8.85*10^{-12}} = 1.13*10^9 m^2$$

$$A = 1.13 * 10^3 km^2 = 1130 km^2$$

Hence, to get capacitance in farads, the area of the plate should be of the order od kilometre which is not good practice, and so that is why ordinary capacitors are of range μF

2.25 <u>Obtain the equivalent capacitance of the network in Figure</u>. For a 300 V supply, <u>determine the charge and voltage across each capacitor</u>.



Answer:

Given.

 $C_1 = 100 pF$

 $C_2 = 200 pF$

 $C_3 = 200 pF$

$$C_4 = 100 pF$$

Now,

Lets first calculate the equivalent capacitance of C_2 and C_3

 $C_{23} = \frac{C_2 C_3}{C_2 + C_3} = \frac{200 * 200}{200 + 200} = 100 pF$

Now let's calculate the equivalent of C_1 and C_{23}

$$C_{1-23} = C_1 + C_{23} = 100 + 100 = 200pF$$

Now let's calculate the equivalent of C_{1-23} and C_4

$$C_{equivalent} = \frac{C_{1-23} * C_4}{C_{1-23} + C_4} = \frac{100 * 200}{100 + 200} = \frac{200}{3} pH$$

Now,

The total charge on C_4 capacitors:

$$Q_4 = C_{equivalent}V = \frac{200}{3} * 10^{-12} * 300 = 2 * 10^{-8}C$$

So,

$$V_4 = \frac{Q_4}{C_4} = \frac{2 * 10^{-8}}{100 * 10^{-12}} = 200V$$

The voltage across C_1 is given by

$$V_1 = V - V_4 = 300 - 200 = 100V$$

The charge on C_1 is given by

$$Q_1 = C_1 V_1 = 100 * 10^{-12} * 100 = 10^{-8} C$$

The potential difference across C_2 and C_3 is

 $V_2 = V_3 = 50V$

Hence Charge on C_2

 $Q_2 = C_2 V_2 = 200 * 10^{-12} * 50 = 10^{-8} C$

And Charge on C_3 :

 $Q_3 = C_3 V_3 = 200 * 10^{-12} * 50 = 10^{-8} C$

2.26 (a) <u>The plates of a parallel plate capacitor have an area of 90 cm² each and are</u> <u>separated by 2.5 mm. The capacitor is charged by connecting it to a 400 V supply.</u>

(a) How much electrostatic energy is stored by the capacitor?

Answer:

Here

The capacitance of the parallel plate capacitor :

$$C = \frac{\epsilon_0 A}{d}$$

The electrostatic energy stored in the capacitor is given by :

Hence, the electrostatic energy stored by the capacitor is $2.55 \ast 10^{-6}J$.

2.26 (b) <u>The plates of a parallel plate capacitor have an area of 90 cm2 each and are</u> separated by 2.5 mm. The capacitor is charged by connecting it to a 400 V supply.

(b) View this energy as stored in the electrostatic field between the plates, and obtain the energy per unit volume u. Hence arrive at a relation between u and the magnitude of electric field E between the plates.

Answer:

The volume of the capacitor is:

$$V = A * d = 90 * 10^{-4}25 * 10^{-3} = 2.25 * 10^{-4}m^3$$

Now,

Energy stored in the capacitor per unit volume :

$$u = \frac{E}{V} = \frac{2.55 * 10^{-6}}{2.55 * 10^{-4}} = 0.113 per m^3$$

Now, the relation between u and E.

2.27 <u>A 4 μF capacitor is charged by a 200 V supply. It is then disconnected from the</u> supply and is connected to another uncharged 2 μF capacitors. How much electrostatic energy of the first capacitor is lost in the form of heat and electromagnetic radiation?

Answer:

Here,

The charge on the capacitance Initially

$$Q = CV = 4 * 10^{-6} * 200 = 8 * 10^{-4}C$$

Total electrostatic energy initially

$$E_{initial} = \frac{1}{2}CV^2 = \frac{1}{2}4 * 10^{-6} * (200)^2 = 8 * 10^{-2}J$$

Now, when it is disconnected and connected to another capacitor

Total new capacitance = $C_{new} = 4 + 2 = 6\mu F$

Now, by conserving the charge on the capacitor:

$$V_{new}C_{new} = C_{initial}V_{initial}$$

$$V_{new} 6\mu F = 4\mu F * 200$$
$$V_{new} = \frac{400}{3}V$$

Now,

New electrostatic energy :

$$E_{new} = \frac{1}{2}C_{new}V_{new}^2 = \frac{1}{2} * 6 * 10^{-6} * \left(\frac{400}{3}\right)^2 = 5.33 * 10^{-2}J$$

Therefore,

Lost in electrostatic energy

$$E = E_{initial} - E_{new} = 0.08 - 0.0533 = 0.0267J$$

2.28 Show that the force on each plate of a parallel plate capacitor has a magnitude equal to $\binom{1}{2}$ QE, where Q is the charge on the capacitor, and E is the magnitude of electric field between the plates. Explain the origin of the factor $\binom{1}{2}$

Answer:

Let

The surface charge density of the capacitor = σ

Area of the plate = A

Now,

As we know,

$$Q = \sigma A \text{ and } E = \frac{\sigma}{\epsilon_0}$$

When the separation is increased by Δx

work done by external force= $F\Delta x$

Now,

Increase in potential energy :

 $\Delta u = u * A \Delta x$

By work-energy theorem,

 $F\Delta x = u * A\Delta x$

$$F = u * A = \frac{1}{2}\epsilon_0 E^2 A$$

putting the value of ϵ_0

$$F = \frac{1}{2}\frac{\sigma}{E}E^2A = \frac{1}{2}\sigma AE = \frac{1}{2}QE$$

origin of 1/2 lies in the fact that field is zero inside the conductor and field just outside is E, hence it is the average value of E/2 that contributes to the force.

2.29 <u>A spherical capacitor consists of two concentric spherical conductors, held in</u> position by suitable insulating supports figure. Show that the capacitance of a spherical $C = \frac{4\pi\epsilon_0 r_1 r_2}{r_1 - r_2}$ where r_1 and r_2 are the radii of outer and inner spheres, respectively.



Answer:

Given

the radius of the outer shell = T_1

the radius of the inner shell = T_2

charge on Inner surface of outer shell = Q

Induced charge on the outer surface of inner shell = -Q

Now,

The potential difference between the two shells

$$V = \frac{Q}{4\pi\epsilon_0 r_2} - \frac{Q}{4\pi\epsilon_0 r_1}$$

Now Capacitance is given by

$$C = \frac{Charge(Q)}{Potential \ difference(V)}$$
$$C = \frac{Q}{\frac{Q(r_1 - r_2)}{4\pi\epsilon_0 r_1 r_2}} = \frac{4\pi\epsilon_0 r_1 r_2}{r_1 - r_2}$$

Hence proved.

2.30 (a) <u>A spherical capacitor has an inner sphere of radius 12 cm and an outer sphere</u> of radius 13 cm. The outer sphere is earthed and the inner sphere is given a charge of 2.5 μ ^C. The space between the concentric spheres is filled with a liquid of dielectric constant 32.

(a) Determine the capacitance of the capacitor.

Answer:

The capacitance of the capacitor is given by:

$$C = \frac{4\pi\epsilon_0\epsilon_r r_1 r_2}{r_1 - r_2}$$

Here,

$$C = \frac{32 * 0.12 * 0.13}{9 * 10^9 * (0.13 - 0.12)} = 5.5 * 10^{-9} F$$

Hence Capacitance of the capacitor is $5.5 * 10^{-9} F$.

2.30 (b) <u>A spherical capacitor has an inner sphere of radius 12 cm and an outer sphere</u> of radius 13 cm. The outer sphere is earthed and the inner sphere is given a charge of $2.5 \ \mu C$. The space between the concentric spheres is filled with a liquid of dielectric constant 32.

(b) what is the potential of the inner sphere?

Answer:

Potential of the inner sphere is given by

$$V = \frac{q}{C} = \frac{2.5 * 10^{-6}}{5.5 * 10^{-9}} = 4.5 * 10^{2}$$

Hence the potential of the inner sphere is $4.5 * 10^2 V$.

2.30 (c) <u>A spherical capacitor has an inner sphere of radius 12 cm and an outer sphere</u> of radius 13 cm. The outer sphere is earthed and the inner sphere is given a charge of 2.5 μ <u>C</u>. The space between the concentric spheres is filled with a liquid of dielectric constant 32.

(c) Compare the capacitance of this capacitor with that of an isolated sphere of radius <u>12 cm. Explain why the latter is much smaller.</u>

Answer:

The radius of the isolated sphere $r = 4.5 * 10^2$

Now, Capacitance of sphere:

 $C_{new} = 4\pi\epsilon_0 r = 4\pi 8.85 * 10^{-12} * 12 * 10^{-12} = 1.33 * 10^{-11} F$

On comparing it with the concentric sphere, it is evident that it has lesser capacitance.this is due to the fact that the concentric sphere is connected to the earth.

Hence the potential difference is less and capacitance is more than the isolated sphere.

Answer carefully:

2.31 (a)

<u>Two large conducting spheres carrying charges Q₁ and Q₂ are brought close to each other. Is the magnitude of electrostatic force between them exactly given by $\frac{Q_1Q_2}{4\pi\epsilon_0r^2}$, where r is the distance between their centres?</u>

Answer:

The charge on the sphere is not exactly a point charge, we assume it when the distance between two bodies is large. when the two charged sphere is brought closer, the charge distribution on them will no longer remain uniform. Hence it is not true that electrostatic force between them exactly given by $\frac{Q_1Q_2}{4\pi\epsilon_0r^2}$.

Answer carefully:

2.31 (b)

If Coulomb's law involved r^3 dependence (instead of r^2), would Gauss's law be still true?

Answer:

Since the solid angle is proportional to $\frac{1}{r^2}$ and not proportional to $\frac{1}{r^3}$,

The guess law which is equivalent of coulombs law will not hold true.

Answer carefully:

2.31 (c)

<u>A small test charge is released at rest at a point in an electrostatic field configuration.</u> <u>Will it travel along the field line passing through that point?</u>

Answer:

when a small test charge is released at rest at a point in an electrostatic field configuration it travels along the field line passing through that point only if the field lines are straight because electric field lines give the direction of acceleration, not the velocity

Answer carefully:

2.31 (d)

What is the work done by the field of a nucleus in a complete circular orbit of the electron? What if the orbit is elliptical?

Answer:

The initial and final position will be the same for any orbit whether it is circular or elliptical. Hence work done will always be zero.

Answer carefully:

2.31 (e)

We know that electric field is discontinuous across the surface of a charged conductor. Is electric potential also discontinuous there?

Answer:

Since the electric potential is not a vector quantity unlike the electric field, it can never be discontinuous.

Answer carefully:

2.31 (f) What meaning would you give to the capacitance of a single conductor?

Answer:

There is no meaning in the capacitor with a single plate factually. but we give it meaning by assuming the second plate at infinity. Hence capacitance of a single conductor is the amount of change required to raise the potential of the conductor by one unit amount.

Answer carefully:

2.31 (g)

<u>Guess a possible reason why water has a much greater dielectric constant (= 80) than</u> <u>say, mica (= 6).</u> Answer:

Water has a much greater dielectric constant than mica because it posses a permanent dipole moment and has an unsymmetrical shape.

2.32 <u>A cylindrical capacitor has two co-axial cylinders of length 15 cm and radii 1.5 cm</u> and 1.4 cm. The outer cylinder is earthed and the inner cylinder is given a charge of 3.5 μ C. Determine the capacitance of the system and the potential of the inner cylinder. Neglect end effects (i.e., bending of field lines at the ends).

Answer:

Given

Length of cylinder l = 15cm

inner radius a = 1.4cm

outer radius b = 1.5cm

Charge on the inner cylinder $q = 3.5 \mu C$

Now as we know,

The capacitance of this system is given by

$$C = \frac{2\pi\epsilon_0 l}{2.303 log_{10}(b/a)}$$
$$C = \frac{2\pi * 8.854 * 10^{-12} * 15 * 10^{-2}}{2.303 log_{10}(1.5 * 10^{-2}/1.4 * 10^{-2})} = 1.21 * 10^{-10} F$$

Now

Since the outer cylinder is earthed the potential at the inner cylinder is equal to the potential difference between two cylinders.

So

Potential of inner cylinder:

$$V = \frac{q}{C} = \frac{3.5 * 10^{-6}}{1.21 * 10^{-10}} = 2.89 * 10^4 V$$

2.33 <u>A parallel plate capacitor is to be designed with a voltage rating 1 kV, using a</u> <u>material of dielectric constant 3 and dielectric strength about $10^{-7}Vm^{-1}$. (Dielectric</u> <u>strength is the maximum electric field a material can tolerate without breakdown, i.e.,</u> <u>without starting to conduct electricity through partial ionisation.)</u> For safety, we should <u>like the field never to exceed, say 10% of the dielectric strength. What minimum area of</u> <u>the plates is required to have a capacitance of 50 pF?</u>

Answer:

Given

Voltage rating in designing capacitor V = 1kV = 1000V

The dielectric constant of the material $K = \epsilon_r = 3$

Dielectric strength of material = $10^7 V/m$

Safety Condition:

$$E = \frac{10}{100} * 10^7 = 10^6 V/m$$

The capacitance of the plate ${\cal C}=50pF$

Now, As we know,

$$E = \frac{V}{d}$$
$$d = \frac{V}{E} = \frac{10^3}{10^6} = 10^{-3}m$$

Now,

$$C = \frac{\varepsilon_0 \varepsilon_r A}{d}$$
$$A = \frac{Cd}{\epsilon_0 \epsilon_r} = \frac{50 * 10^{-12} * 10^{-3}}{8.85 * 10^{-12} * 3} = 1.98 * 10^{-3} m^2$$

Hence the minimum required area is $1.98 * 10^{-3} m^2$

2.34 (a) <u>Describe schematically the equipotential surfaces corresponding to a constant</u> <u>electric field in the z-direction</u>

Answer:

When the electric field is in the z-direction is constant, the potential in a direction perpendicular to z-axis remains constant. In other words, every plane parallel to the x-y plane is an equipotential plane.

2.34 (b) <u>Describe schematically the equipotential surfaces corresponding to a field that</u> <u>uniformly increases in magnitude but remains in a constant (say, z) direction</u>

Answer:

The potential in a direction perpendicular to the direction of the field is always gonna be same irrespective of the magnitude of the electric field. Hence equipotential surface will be the plane, normal of which is the direction of the field. 2.34 (c) <u>Describe schematically the equipotential surfaces corresponding to a single</u> <u>positive charge at the origin, and</u>

Answer:

For a single positive charge, the equipotential surface will be the sphere with centre at position of the charge which is origin in this case.

2.34 (d) <u>Describe schematically the equipotential surfaces corresponding toa uniform</u> grid consisting of long equally spaced parallel charged wires in a plane.

Answer:

The equipotential surface near the grid is periodically varying and after long distance it becomes parallel to the grid.

2.35 <u>A small sphere of radius r 1 and charge q 1 is enclosed by a spherical shell of radius r 2 and charge q2. Show that if q 1 is positive, charge will necessarily flow from the sphere to the shell (when the two are connected by a wire) no matter what the charge q_2 on the shell is.</u>

Answer:

The potential difference between the inner sphere and shell;

$$V = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r_1}$$

So, the potential difference is independent of q_2 . And hence whenever q1 is positive, the charge will flow from sphere to the shell

Answer the following:

2.36 (a)

The top of the atmosphere is at about 400 kV with respect to the surface of the earth, corresponding to an electric field that decreases with altitude. Near the surface of the earth, the field is about 100 Vm^{-1} . Why then do we not get an electric shock as we step out of our house into the open? (Assume the house to be a steel cage so there is no field inside!)

Answer:

The surface of the earth and our body, both are good conductors. So our body and the ground both have the same equipotential surface as we are connected from the ground. When we move outside the house, the equipotential surfaces in the air changes so that our body and ground is kept at the same potential. Therefore we do not get an electric shock.

Answer the following:

2.36 (b)

(b) A man fixes outside his house one evening a two metre high insulating slab carrying on its top a large aluminium sheet of area 1m². Will he get an electric shock if he touches the metal sheet next morning?

Answer:

Yes, the man will get an electric shock. the aluminium sheet is gradually charged up by discharging current of atmosphere.eventually the voltage will increase up to a certain point depending on the capacitance of the capacitor formed by aluminium sheet,

insulating slab and the ground. When the man touches the that charged metal, he will get a shock.

Answer the following:

2.36 (c)

c) The discharging current in the atmosphere due to the small conductivity of air is known to be 1800 A on an average over the globe. Why then does the atmosphere not discharge itself completely in due course and become electrically neutral? In other words, what keeps the atmosphere charged?

Answer:

Thunderstorm and lightning across the globe keep the atmosphere charged by releasing the light energy, heat energy, and sound energy in the atmosphere. In a way or other, the atmosphere is discharged through regions of ordinary weather. on an average, the two opposing currents are in equilibrium. Hence the atmosphere perpetually remains charged.

Answer the following:

2.36 (d)

What are the forms of energy into which the electrical energy of the atmosphere is dissipated during a lightning? (Hint: The earth has an electric field of about $100 Vm^{-1}$ at its surface in the downward direction, corresponding to a surface charge density = $-10^{-9}Cm^{-2}$. Due to the slight conductivity of the atmosphere up to about 50 km (beyond which it is good conductor), about + 1800 C is pumped every second into the earth as a whole. The earth, however, does not get discharged since thunderstorms

and lightning occurring continually all over the globe pump an equal amount of negative charge on the earth.)

Answer:

Electrical energy, of the atmosphere, is dissipated as light energy which comes from lightning, heat energy and sound energy which comes from the thunderstorm.

